



Solucionario

unidad 1

1. Determina si es falso o cierto y escribe por qué:

1) $\sqrt{49} \in \mathbb{Q} \rightarrow \sqrt{49} = \sqrt{7^2} = 7 \in \mathbb{Q} \rightarrow$ **cierto**
 \downarrow
 $49 = 7^2$

2) $2,31331331... \in \mathbb{Q}$

Aunque parece un número irracional, observamos que la terna 331 se empieza a repetir. Por tanto, se podría encontrar la fracción generatriz, ya que se trata de un decimal periódico mixto.

$$\begin{aligned} x &= 2,31\overline{331} \\ 100x &= 231,\overline{331} \\ 100000x &= 231331,\overline{331} \\ \hline 100000x &= 231331,\overline{331} \\ -100x &= 231,\overline{331} \\ \hline 99900x &= 231100 \\ x &= \frac{2311\cancel{00}}{999\cancel{00}} = \frac{2311}{999} \end{aligned}$$

Por tanto, $2,31331331... \in \mathbb{Q} \rightarrow$ **cierto**

3) $\sqrt{6^2 + 4^2} = 7 \rightarrow$ **falso**

$$\left. \begin{aligned} 6^2 &= 36 \\ 4^2 &= 16 \end{aligned} \right\} \begin{aligned} 36 + 16 &= 52 \\ 52 &\neq 49 \end{aligned}$$

$$7^2 = 49$$

4) $\sqrt{16} \in \mathbb{I} \rightarrow$ **falso**

$$\begin{array}{r|l} 16 & 2 \\ 16 = 4^2 & 8 \\ \sqrt{16} = \sqrt{4^2} = 4 & 4 \\ \sqrt{16} \in \mathbb{Q} & 2 \\ & 2 \\ & 1 \end{array}$$

$$16 = 2^4 = 4^2$$

5) $\sqrt{\frac{3}{8}} = 4\sqrt{3} \rightarrow$ **falso**

$$8 = 2^3 \quad ; \quad \sqrt{\frac{3}{2^3}} = \frac{1}{2} \sqrt{\frac{3}{2}} = \frac{1}{2 \cdot 2^2}$$

$$\frac{1}{2} \sqrt{\frac{3}{2}} \neq 4\sqrt{3}$$

6) $\sqrt{300} = 100\sqrt{3} \rightarrow$ **falso**

$$\begin{array}{r|l} 300 & 2 \\ 150 & 2 \\ 75 & 3 \\ 25 & 5 \\ 5 & 5 \\ 1 & 1 \end{array} \quad \begin{array}{l} \text{1 fuera -} \\ \text{0 dentro} \\ \hline \text{1 fuera -} \\ \text{0 dentro} \\ \hline \sqrt{300} = \sqrt{2^2 \cdot 3 \cdot 5^2} = 2 \cdot 5\sqrt{3} = \\ = 10\sqrt{3} \\ 10\sqrt{3} \neq 100\sqrt{3} \end{array}$$

2. Encuentra la fracción generatriz de estos números decimales:

1) 3,21

Primer paso: generar la ecuación.
es un decimal puro

$$\begin{array}{r} x = 3,21 \\ \downarrow \quad \downarrow \\ \times 100 \quad \times 100 \\ \downarrow \quad \downarrow \\ 100x = 321 \end{array}$$

$$x = \frac{321}{100}$$

No se puede simplificar.

$$\left. \begin{array}{l} 100 = 2^2 \cdot 5^2 \\ 321 = 3 \cdot 107 \end{array} \right\} \text{M.C.D. (100, 321) = 1}$$

2) $3,\overline{21}$

$$\begin{array}{r} \downarrow \\ x = 3,\overline{21} \quad \text{es un decimal puro periódico} \\ \downarrow \quad \downarrow \\ \times 100 \quad \times 100 \quad \text{solo extraemos dos de los} \\ \downarrow \quad \downarrow \quad \text{infinitos decimales} \\ 100x = 321,\overline{21} \end{array}$$

Segundo paso: eliminar decimales.

$$\begin{array}{r} 100x = 321,\overline{21} \\ -x = 3,\overline{21} \\ \hline 99x = 318 \\ \times \quad \div \\ x = \frac{318}{99} = \frac{106}{33} \end{array}$$

3) $3,2\overline{1}$

$$\begin{array}{r} \downarrow \\ x = 3,2\overline{1} \\ \downarrow \quad \downarrow \\ \times 10 \quad \times 10 \\ \downarrow \quad \downarrow \\ 10x = 32,\overline{1} \\ \downarrow \quad \downarrow \\ \times 10 \quad \times 10 \\ \downarrow \quad \downarrow \\ 100x = 321,\overline{1} \end{array}$$

$$\begin{array}{r} 100x = 321,\overline{1} \\ -10x = 32,\overline{1} \\ \hline 90x = 289 \\ \times \quad \div \\ x = \frac{289}{90} \end{array}$$

$$\left. \begin{array}{l} 289 = 17^2 \\ 90 = 2 \cdot 3^2 \cdot 5 \end{array} \right\} \text{M.C.D. (289, 90) = 1}$$

3. Opera:

$$1) \left[\underbrace{\left(\frac{3}{2} - \frac{1}{7} \right)}_{1.^\circ} + 5 \underbrace{\left(\frac{2}{3} + 4 \right)}_{2.^\circ} \right] - \left(\frac{5}{2} - 1 \right)$$

1.º

$$a) \frac{3}{2} - \frac{1}{7} = \frac{21-2}{14} = \frac{19}{14}$$

$$\text{m.c.m. (2, 7)} = 2 \cdot 7 = 14$$

$$= 14 \begin{cases} 14 : 2 = 7 \times 3 = 21 \\ 14 : 7 = 2 \times 1 = 2 \end{cases}$$

$$b) \frac{2}{3} + \frac{4}{1} = \frac{2+12}{3} = \frac{14}{3}$$

$$\text{m.c.m. (3, 1)} = 3 \begin{cases} 3 : 3 = 1 \times 2 = 2 \\ 3 : 1 = 3 \times 4 = 12 \end{cases}$$

$$2.^\circ \frac{5}{2} - \frac{1}{1} = \frac{5-2}{2} = \frac{3}{2}$$

$$\text{m.c.m. (2, 1)} = 2 \begin{cases} 2 : 2 = 1 \times 5 = 5 \\ 2 : 1 = 2 \times 1 = 2 \end{cases}$$

$$\left[\frac{19}{14} + \frac{5}{1} \cdot \frac{14}{3} \right] - \frac{3}{2}$$

$$\left[\frac{19}{14} + \frac{5 \cdot 14}{1 \cdot 3} \right] - \frac{3}{2} \quad ; \quad \left[\frac{19}{14} + \frac{70}{3} \right] - \frac{3}{2} =$$

$$\frac{19}{14} + \frac{70}{3} = \frac{980+14}{42} = \frac{70}{3}$$

$$\text{m.c.m. (14, 3)} = 42 \begin{cases} 42 : 14 = 3 \times 19 = 57 \\ 42 : 3 = 14 \times 70 = 980 \end{cases}$$

$$= \frac{70}{3} - \frac{3}{2} = \frac{140-9}{6} = \frac{131}{6}$$

$$\text{m.c.m. (3, 2)} = 3 \times 2 = 6 \begin{cases} 6 : 3 = 2 \times 70 = 140 \\ 6 : 2 = 3 \times 3 = 9 \end{cases}$$

$$\text{solución: } \frac{131}{6}$$

2)

$$3 \times \left(\frac{1}{2} + 0,75 \right) - \left[3 - \frac{1}{6} : \frac{4}{9} \right] + 5$$

$$0,75 \rightarrow \frac{a}{b}?$$

$$x = 0,75$$

$$100x = 75 \quad ; \quad x = \frac{75^{25}}{100^{25}} = \frac{3}{4}$$

$$3 \times \left(\frac{1}{2} + 0,75 \right) - \left[3 - \frac{1}{6} : \frac{4}{9} \right] + 5 =$$

$$\frac{1}{2} + \frac{3}{4} = \frac{2+3}{4} = \frac{5}{4} \quad \frac{1}{6} : \frac{4}{9} = \frac{9 \cdot 1}{6 \cdot 4} = \frac{9}{24}$$

$$\text{m.c.m. } (2, 4) = 4 \begin{cases} 4 : 2 = 2 \times 1 = 2 \\ 4 : 4 = 1 \times 3 = 3 \end{cases}$$

$$= \frac{3}{1} \times \frac{5}{4} - \left[\frac{3}{1} - \frac{9}{24} \right] + 5 =$$

$$= \frac{15}{4} - \frac{63}{24} + \frac{5}{1} \rightarrow \frac{72-9}{24} = \frac{63}{24}$$

$$= \frac{90-63+120}{24} =$$

$$= \frac{147^3}{24^3} = \frac{49}{8}$$

$$\text{m.c.m. } (4, 24) = \begin{cases} 24 : 4 = 6 \times 15 = 90 \\ 24 : 24 = 1 \times 63 = 63 \\ 24 : 1 = 24 \times 5 = 120 \end{cases}$$

$$\text{M.C.D. } (147, 24) = 3$$

$$\text{solución: } \frac{49}{8}$$

3)

$$\frac{0,7\overline{3}-0,25}{1,3\overline{4}}$$

$$x = 0,7\overline{3}$$

$$\downarrow \times 10$$

$$10x = 7,3$$

$$\downarrow \times 10$$

$$100x = 73,3$$

$$100x = 73,3$$

$$-10x = 7,3$$

$$90x = 66$$

$$x = \frac{66^6}{90^6} = \frac{11}{15}$$

$$x = 0,25^{\times 100} \rightarrow 100x = 25$$

$$x = \frac{25^{25}}{100^{25}} = \frac{1}{4}$$

$$x = 1,3\overline{4} \rightarrow 100x = 134,3\overline{4}$$

$$\begin{array}{r} 100x = 134,3\overline{4} \\ -x = 1,3\overline{4} \\ \hline 99x = 133 \end{array}$$

$$x = \frac{133}{99}$$

$$\frac{0,7\overline{3}-0,25}{1,3\overline{4}} = \frac{\frac{11}{15}-\frac{1}{4}}{\frac{133}{99}} = \frac{\frac{29}{60}}{\frac{133}{99}} \Rightarrow$$

$$\Rightarrow \frac{29}{60} : \frac{133}{99} = \frac{29 \cdot 99}{60 \cdot 133}$$

$$\frac{11}{15} - \frac{1}{4} = \frac{44-15}{60} = \frac{29}{60}$$

$$\text{m.c.m. } (15, 4) = 60 \begin{cases} 60 : 15 = 4 \times 11 = 44 \\ 60 : 4 = 15 \times 1 = 15 \end{cases}$$

$$= \frac{2871^3}{7980^3} = \frac{957}{2660}$$

$$\text{M.C.D. } (2871, 7980) = 3$$

$$\text{solución: } \frac{957}{2660}$$

$$4) \quad 1 - \frac{1}{2 - \frac{1}{1 + \frac{2}{3}}} = 1 - \frac{1}{2 - \frac{1}{\frac{5}{3}}} = 1 - \frac{1}{\frac{7}{5}} \times = 1 - \frac{5}{7}$$

$$1 + \frac{2}{3} = \frac{3+2}{3} = \frac{5}{3} \quad ; \quad \frac{2}{1 - \frac{1}{\frac{5}{3}}} \times = \frac{10-3}{5} = \frac{7}{5}$$

$$1 - \frac{5}{7} = \frac{7-5}{7} = \frac{2}{7}$$

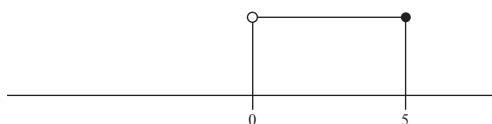
$$\text{solución: } \frac{2}{7}$$

4. Representa en la recta de los números reales los siguientes intervalos:

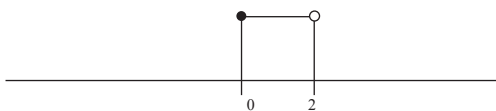
1) $[-7, 3]$



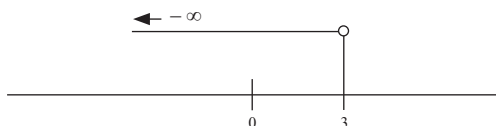
2) $(0, 5]$



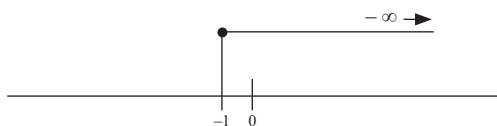
3) $0 \leq x < 2$



4) $(-\infty, 3)$

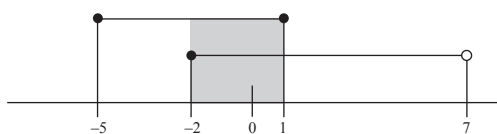


5) $[-1, +\infty)$

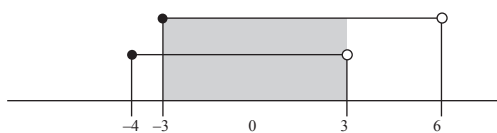


5. Representa y determina el intervalo resultante de las siguientes operaciones:

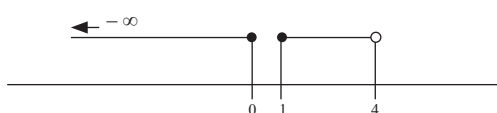
1) $[-5, 1] - [-2, 7) = [-2, 1]$



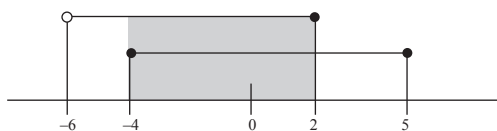
2) $[-3, 6) - [-4, 3) = [-3, 3)$



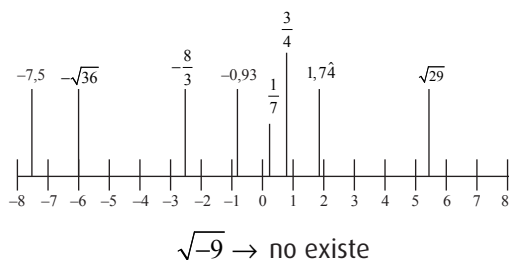
3) $(-\infty, 0] - [1, 4) = 0$



4) $(-6, 2] - [-4, 5] = [-4, 2]$



6. Representa en la recta de los números reales los siguientes valores:



7. Dados los siguientes valores, redondea y trunca según se indica y calcula el error absoluto y relativo que generan:

1) 0,7398415 a las centésimas

redondeo: 0,74

truncamiento: 0,73

$$E_{abs} = |0,74 - 0,7398415| = 0,0001585$$

$$E_r = \frac{0,0001585}{0,7398415} \times 100 = 0,0214\%$$

2) 6,19132584 a las décimas

redondeo: 6,2

truncamiento: 6,1

$$E_{abs} = |6,2 - 6,19132584| = 0,00867416$$

$$E_r = \frac{0,00867416}{6,19132584} \times 100 = 0,14\%$$

3) 4,38965531 a las milésimas

redondeo: 4,390

truncamiento: 4,389

$$E_{abs} = |4,390 - 4,38965531| = 0,000345$$

$$E_r = \frac{0,000345}{4,38965531} \times 100 = 0,0079\%$$

4) 0,00371982 a las diezmilésimas

redondeo: 0,0037

truncamiento: 0,0037

$$E_{abs} = |0,0037 - 0,00371982| = 0,000019821 = 1,9821 \times 10^{-5}$$

$$E_r = \frac{1,9821 \times 10^{-5}}{0,00371982} \times 100 = 0,53\%$$

8. Calcula:

a) $\frac{5}{9} - \left[\underbrace{-\frac{3}{4} + \frac{1}{2}}_{1.^o} + \frac{10}{2} \cdot \underbrace{\left(\frac{1}{2} - \frac{3}{5} \right)}_{2.^o} \right] =$

$$1.^o \quad -\frac{3}{4} + \frac{1}{2} = \frac{-3+2}{4} = \frac{-1}{4}$$

m.c.m. (4, 2) = 4

$$2.^o \quad \frac{1}{2} - \frac{3}{5} = \frac{5-6}{10} = \frac{-1}{10}$$

m.c.m. (2, 5) = 10

$$= \frac{5}{9} - \left[\underbrace{\left(-\frac{1}{4} \right)}_{- \cdot - = +} + \frac{10}{2} \cdot \underbrace{\left(\frac{-1}{10} \right)}_{\times} \right] = \frac{5}{9} + \frac{1}{4} + \left(\frac{1 \cancel{0} \cdot -1}{2 \cdot 1 \cancel{0}} \right) =$$

$$= \frac{5}{9} + \frac{1}{4} + \left(-\frac{1}{2} \right) = \frac{5}{9} + \frac{1}{4} - \frac{1}{2} = \frac{20+9-17}{36} =$$

+ · - = -

$$= \frac{29-17}{36} = \frac{12}{36} = \frac{1}{3}$$

$$\text{m.c.m. (9, 4, 2)} = 36 \begin{cases} 36 : 9 = 4 \times 5 = 20 \\ 36 : 4 = 9 \times 1 = 9 \\ 36 : 2 = 18 \times 1 = 18 \end{cases}$$

$$\text{solución: } \frac{1}{3}$$

$$\text{b) } \frac{3}{8} \cdot \underbrace{\left(\frac{5}{3} - \frac{1}{2} \right)}_{1.^\circ} - \frac{4}{11} \cdot \underbrace{\left(\frac{3}{4} - \frac{1}{5} \right)}_{2.^\circ} = \frac{3}{8} \cdot \left(\frac{7}{6} \right) - \frac{4}{11} \cdot \left(\frac{11}{20} \right)$$

$$1.^\circ \quad \frac{5}{3} - \frac{1}{2} = \frac{10-3}{6} = \frac{7}{6}$$

$$\text{m.c.m. (3, 2)} = 6 \begin{cases} 6 : 3 = 2 \times 5 = 10 \\ 6 : 2 = 3 \times 1 = 3 \end{cases}$$

$$2.^\circ \quad \frac{3}{4} - \frac{1}{5} = \frac{15-4}{20} = \frac{11}{20}$$

$$\text{m.c.m. (4, 5)} = 20 \begin{cases} 20 : 4 = 5 \times 3 = 15 \\ 20 : 5 = 4 \times 1 = 4 \end{cases}$$

$$= \frac{3 \cdot 7}{8 \cdot 6} - \frac{4 \cdot 11}{11 \cdot 20} = \frac{21}{48} - \frac{4}{20} = \frac{105-48}{240} = \frac{57}{240}$$

$$\begin{cases} 48 = 2^4 \cdot 3 \\ 20 = 2^2 \cdot 5 \end{cases} \text{m.c.m. (48, 20)} = 2^4 \cdot 3 \cdot 5 =$$

$$= 240 \begin{cases} 240 : 48 = 5 \times 21 = 105 \\ 240 : 20 = 12 \times 4 = 48 \end{cases}$$

$$\text{solución: } \frac{19}{80}$$

$$\text{M.C.D. (57, 240)} = 3$$

9. Efectúa:

$$\text{a) } 5 - \underbrace{(-2)}_{- \cdot - = +} + \underbrace{(-8) : (-4)}_{- \cdot - = +} - 5 =$$

2

$$= 5 + 2 + 2 - 5 = 4$$

$$\text{b) } \underbrace{-6 : 2}_{- \cdot + = -} + \underbrace{(-7) \cdot (-15)}_{- \cdot - = +} : 3$$

(-7) · (-5)

- · - = +

$$-3 + 35 = 32$$

$$\text{c) } 7 - 3 - \underbrace{(-8) : (-4)}_{- \cdot - = +} + \underbrace{(-9) : (-3)}_{- \cdot - = +}$$

+ · - = -

-2

$$7 - 3 - 2 + 3 = 5$$

10. Expresa en forma fraccionaria y resuelve:

$$\text{a) } \frac{(1,3+1,87)^2}{1,75} - \frac{6}{(2,3+0,7)^2 - (0,85)^3}$$

$$x = 1,3 \xrightarrow{\times 10} 10x = 13 \rightarrow x = \frac{13}{10}$$

$$x = 1,87 \xrightarrow{\times 100} 100x = 187 \rightarrow x = \frac{187}{100}$$

$$x = 1,75 \xrightarrow{\times 100} 100x = 175 \rightarrow x = \frac{175}{100} = \frac{7}{4}$$

$$x = 2,3 \xrightarrow{\times 10} 10x = 23 \rightarrow x = \frac{23}{10}$$

$$x = 0,7 \xrightarrow{\times 10} 10x = 7 \rightarrow x = \frac{7}{10}$$

$$x = 0,85 \xrightarrow{\times 100} 100x = 85 \rightarrow x = \frac{85}{100} = \frac{17}{20}$$

$$\frac{\left(\frac{13}{10} + \frac{187}{100} \right)^2}{\frac{7}{4}} - \frac{6}{\left(\frac{23}{10} + \frac{7}{10} \right)^2 - \left(\frac{17}{20} \right)^3} =$$

$$\frac{13}{10} + \frac{187}{100} = \frac{130+187}{100} = \frac{317}{100} \rightarrow \left(\frac{317}{100} \right)^2 =$$

$$= \frac{100489}{10000} \quad \text{m.c.m. (10, 100)}$$

$$\frac{23}{10} + \frac{7}{10} = \frac{30}{10} = 3 \rightarrow 3^2 = 9$$

$$\left(\frac{17}{20}\right)^3 = \frac{4913}{8000}$$

$$= \left[\frac{100489}{\frac{10000}{\frac{7}{4} \times}} - \frac{6}{9 - \left(\frac{4913}{8000}\right)} = \frac{401956}{70000} - \right.$$

$$\left. - \frac{6}{\frac{72000 - 4913}{8000}} \right] \times$$

$$\text{m.c.m. (1, 8000)} = 8000$$

$$= \frac{401956}{70000} - \frac{48000}{67087} =$$

$$= \frac{26966022172 - 3360000000}{4696090000} =$$

$$= \frac{23606022172^4}{4696090000^4} =$$

$$= \frac{5901505543}{1174022500}$$

$$70000 = 2^4 \cdot 5^4 \cdot 7$$

$$67087 = 67087$$

b) $0,0\hat{9} : 0,3\hat{3} - 0,11 : 0,3 - \sqrt{0,5} \cdot 2 + 0,6\hat{5} \cdot 3,1$

$$x = 0,0\hat{9} \rightarrow 10x = 0,9 \rightarrow 100x = 9,9$$

$$\begin{array}{r} 100x = 9,9 \\ -10x = 0,9 \\ \hline 90x = 9 \end{array} \quad x = \frac{9}{90} = \frac{1}{10}$$

$$x = 0,3\hat{3} \rightarrow 10x = 3,3$$

$$\begin{array}{r} 10x = 3,3 \\ -x = 0,3 \\ \hline 9x = 3 \end{array} \quad x = \frac{3}{9} = \frac{1}{3}$$

$$x = 0,11 \rightarrow 100x = 11 \quad ; \quad x = \frac{11}{100}$$

$$x = 0,3 \rightarrow 10x = 3 \quad ; \quad x = \frac{3}{10}$$

$$x = 0,5\hat{5} \rightarrow 10x = 5,5$$

$$\begin{array}{r} 10x = 5,5 \\ -x = 0,5 \\ \hline 9x = 5 \end{array} \quad x = \frac{5}{9}$$

$$x = 0,6\hat{5} \rightarrow 100x = 65,6\hat{5}$$

$$\begin{array}{r} 100x = 65,6\hat{5} \\ -x = 0,6\hat{5} \\ \hline 99x = 65 \end{array} \quad x = \frac{65}{99}$$

$$x = 3,1 \rightarrow 10x = 31$$

$$x = \frac{31}{10}$$

$$\begin{aligned} & \frac{1}{10} : \frac{1}{3} - \frac{11}{100} : \frac{3}{10} - \sqrt{\frac{5}{9}} \cdot 2 + \frac{65}{99} : \frac{31}{10} \\ & \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \\ & \frac{3}{10} - \frac{110}{300} - \sqrt{\frac{10}{9}} + \frac{650}{3069} = \\ & = \frac{920700 - 112530 + 65000}{61380} - \sqrt{\frac{10}{9}} = \end{aligned}$$

$$\left. \begin{array}{l} 10 = 2 \cdot 5 \\ 300 = 2^2 \cdot 3 \cdot 5^2 \\ 3069 = 3^2 \cdot 11 \cdot 31 \end{array} \right\}$$

$$\text{m.c.m. (10, 300, 3069)} = 2^2 \cdot 5^2 \cdot 3^2 \cdot 11 \cdot 31 = 306900$$

$$\left\{ \begin{array}{l} 306900 : 10 = 30690 \times 3 = 920700 \\ 306900 : 300 = 1023 \times 110 = 112530 \\ 306900 : 3069 = 100 \times 650 = 65000 \end{array} \right.$$

$$= \frac{873170}{61380} - \sqrt{\frac{10}{9}} = \frac{87317}{6138} - \sqrt{\frac{10}{9}}$$

11. Resuelve los siguientes problemas:

- a)** Un coche recorre 70 kilómetros en tres cuartos de hora y otro recorre 41 kilómetros en 28 minutos. ¿Cuál es el más rápido?

A: 70 km. - $\frac{3}{4}$ horas \rightarrow 70 km. \rightarrow 45 min.

B: 41 km. - 28 min. \rightarrow 41 km. \rightarrow 28 min.

$$\frac{3}{4} \text{ horas} \rightarrow \frac{3}{4} \text{ horas} \cdot \frac{60 \text{ minutos}}{1 \text{ hora}} = \frac{180}{4} = 45$$

$$\left. \begin{array}{l} \frac{70 \text{ km.}}{45 \text{ min.}} = 1,56 \text{ km./min.} \\ \frac{41 \text{ km.}}{28 \text{ min.}} = 1,46 \text{ km./min.} \end{array} \right\} \begin{array}{l} \text{el vehículo A es} \\ \text{el más rápido} \end{array}$$

